



- d. Assuming that the height increases at the constant rate of 3 in. per year, does the weight also increase at a constant rate? Explain how you arrived at your answer.
- e. What is a reasonable domain for  $t$  for the composite function  $W \circ h$ ?
- f. *Composite Functions Numerically Problem:* Functions  $f$  and  $g$  are defined only for the values of  $x$  in the table.

$x$	$f(x)$	$g(x)$
3	2	4
4	6	5
5	3	8
6	5	3

Find these values, or explain why they are undefined:  $f(g(3))$ ,  $f(g(4))$ ,  $f(g(5))$ ,  $f(g(6))$ ,  $g(f(6))$ ,  $f(f(3))$ , and  $g(g(3))$ .

*Two Linear Functions Problem:* For parts g–j, let functions  $f$  and  $g$  be defined by

$$f(x) = x - 2 \quad 4 \leq x \leq 8$$

$$g(x) = 2x - 3 \quad 2 \leq x \leq 6$$

- g. Plot the graphs of  $f$ ,  $g$ , and  $f(g(x))$  on the same screen. Sketch the results.
- h. Find  $f(g(4))$ .
- i. Show that  $f(g(3))$  is undefined, even though  $g(3)$  is defined.
- j. Calculate the domain of the composite function  $f \circ g$  and show that it agrees with the graph you plotted in part g.

- R5. Figure 1-8i shows the graph of  $f(x) = x^2 + 1$  in the domain  $-1 \leq x \leq 2$ .

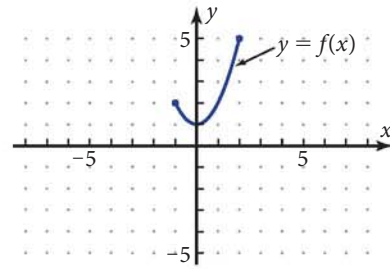


Figure 1-8i

- a. On a copy of the figure, sketch the graph of the inverse relation. Explain why the inverse is not a function.
- b. Plot the graphs of  $f$  and its inverse relation on the same screen using parametric equations. Also plot the line  $y = x$ . How are the graphs of  $f$  and its inverse relation related to the line  $y = x$ ? How are the domain and range of the inverse relation related to the domain and range of function  $f$ ?
- c. Write an equation for the inverse of the function  $y = x^2 + 1$  by interchanging the variables. Solve the new equation for  $y$  in terms of  $x$ . How does this solution reveal that there are two different  $y$ -values for some  $x$ -values?
- d. On a copy of Figure 1-8j, sketch the graph of the inverse relation. What property does the function graph have that allows you to conclude that the function is invertible? What are the vertical lines at  $x = -3$  and at  $x = 3$  called?

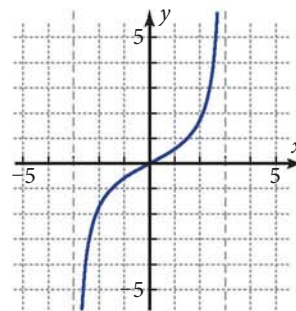


Figure 1-8j